



OBSTACLE AVOIDANCE METHOD FOR A GROUP OF HUMANOIDS INSPIRED BY SOCIAL FORCE MODEL

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Abstract

This paper presents a new formulation for obstacle and collision behavior on a group of humanoid robots that adopts walking behavior of pedestrian crowd. A pedestrian receives position information from the other pedestrians, calculate his movement and then continuing his objective. This capability is defined as socio-dynamic capability of a pedestrian. Pedestrian's walking behavior in a crowd is an example of a sociodynamics system and known as Social Force Model (SFM). This research is trying to implement the avoidance terms in SFM into robot's behavior. The aim of the integration of SFM into robot's behavior is to increase robot's ability to maintain its safety by avoiding the obstacles and collision with the other robots. The attractive feature of the proposed algorithm is the fact that the behavior of the humanoids will imitate the human's behavior while avoiding the obstacle. The proposed algorithm combines formation control using Consensus Algorithm (CA) with collision and obstacle avoidance technique using SFM. Simulation and experiment results show the effectiveness of the proposed algorithm.

Keywords: humanoid robots; formation control; obstacle avoidance; social force model; consensus algorithm.

I. INTRODUCTION

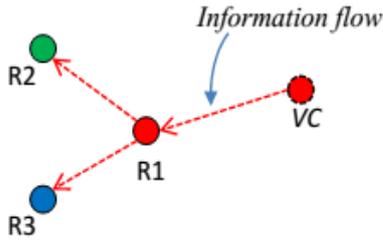
This paper propose a new approach to solve obstacle avoidance problem on a group of humanoid robots by combining of consensus algorithm and sociodynamic approach. Sociodynamics is a systematic approach to mathematical modeling in the social sciences. Sociodynamics has been developed starting from interdisciplinary approach that attempts to model the dynamic behavior of the social system of stochastic and quasi-deterministic models into more structured physical-mathematical system. The term of socio-dynamic is introduced by Weidlich, as quoted in [1].

The goal of this new approach is to make a group of humanoid robots can walk to desired position and still able to avoid obstacle while still maintaining their path to their desired position. The new approach is using Social Force Model

(SFM) approach to make robots able to avoid obstacle and collision. SFM itself is a pedestrian's walking behavior dynamic mathematical model developed by Helbing and Molnar [2]. The implementation of human behavior in humanoid's behavior is based on the premise that, in the next few years, a humanoid robot will be placed on the human environment. So, if a robot will be placed in a human environment/crowd, it must have some knowledge of human behavior and capable to imitate and calculate it into its behavior.

By using the SFM, the robot's walking behavior is expected to be able to imitate the behavior of pedestrians in a crowd. The social force captures the effect of the neighboring pedestrians and the environment on the movement of individuals in the crowd. Helbing [2] used the SFM approach into collective model of social panic to simulate the behavior of an escape panic of a crowd. In this model, both

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VC = Virtual Center as virtual reference

Figure 3. Communication topology from the virtual center to all robots in the system

Given the initial configuration as shown in Figure 1, the objective of the system are:

- All robot can walk from an initial position to their desired position, in a certain formation. R1, R2, and R3 are placed on the left side, and R4 is placed on the right side of the experimental platform. A control input u_i will make i -th robot walks from r_i to r_i^d as $t \rightarrow \infty$.
- All robots can avoid obstacle while they walk along the way to reach their desired destination.
- For obstacle avoidance, collision and obstacle avoidance factor from SFM equation were used.

By using the observation results of Moussaïd *et al.* [5] as a comparison, the expected results of the experiment of this new algorithm will resemble the behavior as depicted in Figure 4. Figure 4 shows the results of computer simulations for the heuristic pedestrian model (solid lines) compared with experimental results (shaded lines) during simple avoidance maneuvers in a corridor. Part (A) shows the average trajectory of a pedestrian passing a static obstacle in the middle of the corridor; and part (B) shows the average trajectory of a pedestrian passing another individual moving in the opposite direction.

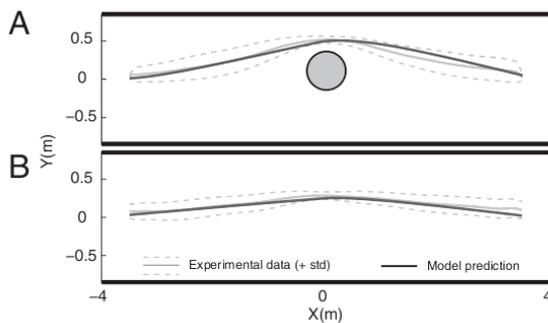


Figure 4. Comparison between simulations with experimental results of the heuristic pedestrian walking model during simple avoidance maneuvers in a corridor [6]

III. METHOD

This section describes the method that is used to solve the problem, begin with the basic theory of SFM, CA for formation control, obstacle/collision avoidance techniques and stability analysis.

A. Social Force Model

According to Helbing *et al.* [2], the motion behavior of a pedestrian is determined by some factors, which are: (i) individual desired direction, (ii) some influences from other pedestrians, (iii) some influences from obstacles, walls or other objects, and (iv) influence of an attractive object. The general SFM equation can be written as:

$$F_i(t) = F_i^0(v_i, v_i^0 e_i) + \sum_j F_{ij}(e_i, r_i - r_j) + \sum_o F_{io}(e_i, r_i - r_o^i) + \sum_a F_{ia}(e_i, r_i - r_a^i) \quad (3)$$

The first term, $F_i^0(v_i, v_i^0 e_i)$, in equation (3) represents pedestrian's individual desired direction, where v_i, v_i^0 , and e_i represents, respectively, actual speed, desired speed, and desired direction of pedestrian i . The second term, $F_{ij}(e_i, r_i - r_j)$ represents the influence of other pedestrian to pedestrian i , where r_i and r_j represent position of pedestrian i and j . In particular, the pedestrian keeps a certain distance from other pedestrian and to avoid collision, depends on the desired speed (v_i^0) and pedestrian density. A repulsive effect of other pedestrian j is denoted in this term. The third and fourth term represent, respectively, a repulsive effects of an obstacle $F_{io}(e_i, r_i - r_o^i)$ and an attractive effect of an attractive object/person, $F_{ia}(e_i, r_i - r_a, t)$. Pedestrians are sometimes attracted by other persons (friends, street artists, commercials, etc).

Since research focus on obstacle/collision avoidance behavior and formation control, the fourth term from equation (3) was excluded. So, by using this simplification and equation in [3], the avoidance behavior part of SFM is written as:

$$\sum_j F_{ij}(e_i, r_{ij}) = w_d C_d e^{0.5 \sqrt{(\|r_{ij}\| + \|r_{ij}-s\|)^2 - s^2}} \quad (4)$$

and

$$\sum_o F_{io}(e_i, r_i - r_o^i) = w_s C_s e^{(r_i - r_{obs})/B} \quad (5)$$

where B, C_s, C_d are positive scalar, $r_{ij} \triangleq (r_i - r_j)$, s is step distance of the robot and r_{obs} is position of an obstacle.

The repulsive effects of equations (4) and (5) only hold for situation that are perceived in the

pedestrian's field of view ($FOV, 2\varphi$). In order to take this effect of perception into account, it need to introduce the direction dependent weights w_s and w_d :

$$w(\vec{e}, \vec{f}) := \begin{cases} 1, & \text{if } \vec{e} \cdot \vec{f} \geq \|\vec{f}\| \cos\varphi \\ c, & \text{otherwise.} \end{cases} \quad (6)$$

By replacing (4) and (5) into (3), SFM equation can be derived as:

$$F_i(t) = F_i^0(v_i, v_i^0 e_i) + \sum_0 w_s C_s e^{(r_i - r_{obs})/B} + \sum_j w_d C_d e^{0.5 \sqrt{(\|r_i - r_j\| + \|r_i - r_j - s\|)^2 - s^2}} \quad (7)$$

Comparing with the other obstacle/collision avoidance equations which were used in some algorithms [6-9], the use of FOV in this algorithm will become a distinctive factor, with the others. In the experiment, the value of φ is set to 60° . The avoidance behavior of the robots should be acted differently.

The first term of equation (7) is the formation control term which will maintain robot position on a formation or still keeping them in a group. This formation control term will be described in the next section.

B. Consensus Algorithm for Formation Control

Consensus algorithm (CA) is a distributed control algorithm for multi-agent systems, which allow each agent in the system to achieve agreement with the other agents by sharing its information states. CA is a major method to solve many multi-agent cooperative control problems. Currently, CA has been developed and used in many applications of multi-robot systems. This is because the algorithm is distributive, so that the control equation for the robot can be simpler than the centralized control method.

A necessary condition to achieve consensus is the availability of a communication topology that allow the information states are shared to all member of the group. If a communication

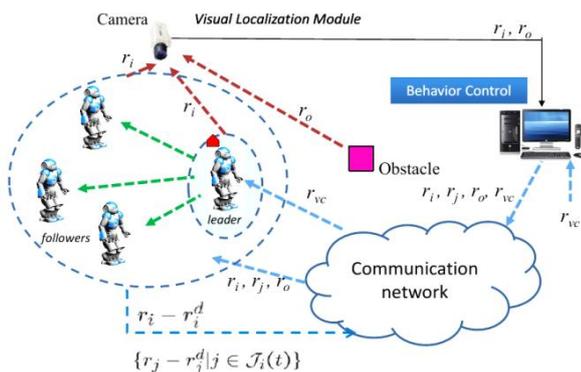


Figure 5. Illustration of the experiment

topology in a multi-robots system is established for all robots, then consensus will be achieved if and only if the topology has a spanning tree [4].

In the case of formation establishment and control, some information states are needed to be shared. In this paper, virtual structure (VS) approach to solve the formation control problems was used. Using this approach, the entire formation is treated as a rigid body or single structure, and then, the control strategy is derived in three stages [3]:

1. Stage 1: define the desired dynamics of the virtual leader/virtual center of a virtual structure. This stage is illustrated in Figure 1.
2. Stage 2: translate the motion of the virtual leader/virtual center into desired motion for each robot. This stage is also illustrated in Figure 1.
3. Stage 3: derive tracking controls for each robot.

Since the research used 4 robots, a triangle formation for the group of 3 robots (R1, R2, and R3) was defined. The 4th robot will be acted as dynamic obstacle. In the group, the information states are shared to all robots by using communication topology depicted in Figure 3, while R4 received the position of the other robots and the obstacle.

All information states (i.e. r_i, r_j, r_{obs}) are provided by a Visual Localization Module (VLM), which consists of a web camera and a PC. VLM uses visual odometry (VO) technique to obtain all robots and obstacle positions and then share it to all robots. By taking the capability of robots used in the experiment into account, VO is regarded as the most appropriate technique to apply in the experiment. The illustration of the experiment is depicted in Figure 5. The algorithm of VO technique is depicted in Figure 6.

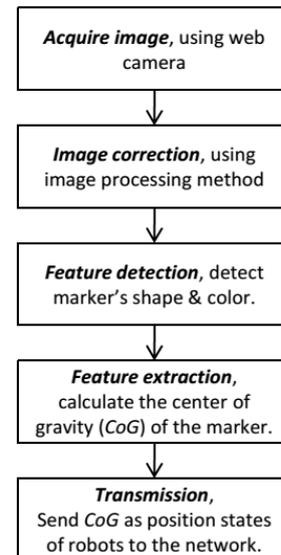


Figure 6. The algorithm of visual odometry technique

For stage 3 of the VS approach, CA equation for reference tracking was used, which can be written as in equation (8). All position states (r_i, r_j, r_{obs}) are obtained by using VO.

$$u_i = \dot{r}_i^d - \alpha_i(r_i - r_i^d) - \sum_{j=1}^n a_{ij}[(r_i - r_i^d) - (r_j - r_j^d)] \quad (8)$$

where α_i is a positive scalar, a_{ij} is the (i, j) entry of adjacency matrix A_n associated with communication topology G_n and $r_i^d = [x_i^d, y_i^d]^T$ is the i -th robot's desired position. While, $r_i - r_i^d$ and $r_j - r_j^d$ represents respectively, distance between the i -th robot's actual and desired position, the j -th robot's actual and desired position.

C. Obstacle/Collision Avoidance Technics

To implement SFM into robot's behavior, CA equation (8) was integrated into equation (7), so that equation (7) is expanded to equation (9).

$$u_i = \dot{r}_i^d - \alpha_i(r_i - r_i^d) - \sum_{j=1}^n a_{ij}[(r_i - r_i^d) - (r_j - r_j^d)] + w_s C_s e^{(r_i - r_{obs})/B} + w_d C_d e^{0.5\sqrt{(\|r_{ij}\| + \|(r_{ij}) - s\|)^2 - s^2}} \quad (9)$$

Equation (9) is the final equation to be implemented into humanoids robot. The obstacle and collision avoidance force are respectively presented by the fourth and fifth term of equation (9). The stability analysis of this algorithm is derived by using Lyapunov's stability analysis and will be explained in the next subsection.

To implement equation (9) to robot, it need 2 more processes, which are: frame coordinate transformation and limitation process of the robot's steps and orientation. Since robot Nao has some limitation on its moves, the research try to imitate pedestrian's walking behavior that is tend to be a non-holonomic behavior, treat and reprogram Nao as a non-holonomic robot. To make a leg movement on Nao, control input given by equation (9) must not exceed robot's maximum foot step parameters, which are 0.08 m to step forward (X-axis) and 0.06 m to step aside (Y-axis). Control input u_i is transformed into foot step u_{ix} and u_{iy} where $u_{ix} \leq 0.08$ and $u_{iy} \leq 0.06$. By using this foot step parameter, the robot's maximum steps is set to $s_j = 0.08$. As a result, robot will move in its maximum velocity if $u_{ix} > 0.08$ or $u_{iy} > 0.06$.

D. Stability Analysis

In this subsection, will be carried out analysis of the stability of equation (9). The purpose of this analysis is examining equation (9), to ensure the robot able to avoid obstacles and still

returning to its mission toward its desired destination. The analysis was performed using Lyapunov stability analysis approach. To understand the analysis, some assumptions and definition are needed. Throughout this section, a system of nonlinear differential equations was considered.

$$\dot{x} = f(x), \quad x(t_0) = 0 \quad (10)$$

where $x, x_0 \in \mathbb{R}^n$ and $f(\cdot): \mathbb{R}^n \rightarrow \mathbb{R}^n$.

1) Definition

a) Equilibrium point (x^*) :

x^* is said to be an equilibrium point of equation (10) if $f(x^*) = 0$.

b) Stable Equilibrium:

The equilibrium point $x^* = 0$ is said to be a *stable* point of equation (10) if, for all $\epsilon > 0$, there exists a $\delta(\epsilon)$ such that $\|x_0\| < \delta(\epsilon) \Rightarrow \|x(t)\| < \epsilon, \forall t \geq t_0$ where $x(t)$ is the solution of equation (10).

c) Asymptotic Stability:

The equilibrium point $x^* = 0$ is said to be an *asymptotically stable* point of (10) if:

- it is stable;
- it is attractive, i.e. there exists a δ such that:

$$\|x_0\| < \delta \Rightarrow \lim_{t \rightarrow \infty} \|x(t)\| = 0,$$

where $x(t)$ is the solution of equation (10). Note that (a) above does not necessarily imply (b).

d) Locally Positive Definite Function:

A continuous function $V(x): \mathbb{R}^n \rightarrow \mathbb{R}^+$ is called a locally positive definite function if, for some $h > 0$ and $\alpha(\cdot), V(0) = 0$ and $V(x) \geq \alpha(\|x\|) \forall x: \|x\| < h$ where $\alpha(\cdot): \mathbb{R}^n \rightarrow \mathbb{R}^+$ is continuous, strictly increasing, and $\alpha(0) = 0$.

2) Assumptions

- The robot's radii (R_{robot}) is 0.2 m.
- The maximum robot's walking step (s_j^{max}) is 0.08 m.

Following the works of [4] and [10], analysis is started by noting that:

$$F_i = F_i^{att} + F_i^{rep} \quad (11)$$

where F_i^{att} is the attractive potential function and F_i^{rep} is the repulsive potential function of the i -th robot. Intuitively and necessarily, potential functions should have the properties that.

$$\begin{cases} F_i^{att}(0) = 0, & \nabla F_i^{att}(r_i - r_i^d)|_{(r_i - r_i^d)=0} = 0, \\ 0 < F_i^{att}(r_i - r_i^d) < \infty, & \text{if } \|r_i - r_i^d\| \neq 0 \text{ is finite,} \\ \|\nabla F_i^{att}(r_i - r_i^d)\| < +\infty & \text{if } \|r_i - r_i^d\| \text{ is finite} \end{cases} \quad (12)$$

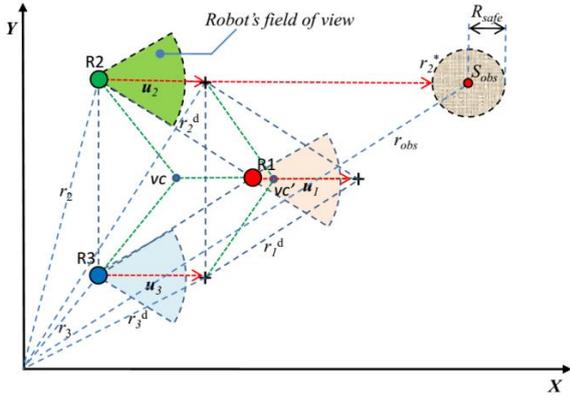


Figure 7. Illustration of obstacle/collision avoidance and formation control

and

$$\begin{cases} F_i^{rep}(r_i - r_{obs}) = 0, & \text{if } (r_i - r_{obs}) \notin S_{obs}, \\ F_i^{rep}(r_i - r_{obs}) \in (0, \infty), & \text{if } (r_i - r_{obs}) \in S_{obs}. \end{cases} \quad (13)$$

It can be defined that:

1. $F_i^{att} > F_i^{rep}$, if $\|r_i - r_{obs}\| > R_{safe}$,
2. $F_i^{att} < F_i^{rep}$, if $\|r_i - r_{obs}\| < R_{safe}$,
3. $F_i^{att} = -F_i^{rep}$, if $\|r_i - r_{obs}\| = R_{safe} \Rightarrow$ equilibrium point (r_i^*).

where S_{obs} is an area around the obstacle, defined as a circle with a radius R_{safe} .

This condition is illustrated in Figure 7. Since this paper focuses on obstacle/collision avoidance, only F_i^{rep} term was considered for analysis. Using properties in equation (11) can be rewrote to equation (10) where:

$$u_i^{rep} = w_s C_s e^{(r_i - r_{obs})/B} + w_d C_d e^{0.5 \sqrt{(\|r_i - r_j\| + \|(r_i - r_j) - s_j\|)^2 - s_j^2}} \quad (14)$$

Focused on obstacle/collision avoidance term, define Lyapunov-like function candidate for (14)

as $V = u_i^{rep}$, where:

$$V = w_s C_s e^{\frac{(r_i - r_{obs})}{B}} + w_d C_d e^{0.5 \sqrt{(\|r_{ij}\| + \|r_{ij} - s_j\|)^2 - s_j^2}} \quad (15)$$

Assumption III.1 implies that $r_{ij} > 2R_{Robot} > s_j$. Because w_s, w_d, C_s , and C_d are positive scalar, it is obvious that V is a positive definite function. To find the derivative function of V, V should be seen as $V = V^a + V^b$ where :

$$V^a = w_s C_s e^{(r_i - r_{obs})/B}, \quad (16)$$

$$V^b = w_d C_d e^{0.5 \sqrt{(\|r_i - r_j\| + \|(r_i - r_j) - s_j\|)^2 - s_j^2}} \quad (17)$$

Then, by using derivative calculation, the derivative functions of V^a and V^b are given by:

$$\dot{V}^a = -\frac{w_s C_s}{B} e^{-\|r_i - r_{obs}\|/B} < 0 \quad (18)$$

and

$$\dot{V}^b = -0.5 w_d C_d e^{-0.5 \sqrt{(\|r_{ij}\| + \|r_{ij} - s_j\|)^2 - s_j^2}} \left(\frac{\|r_{ij}\| - s_j}{\|s_j - r_{ij}\|} + \frac{r_{ij}}{\|r_{ij}\|} \right) (\|s_j - r_{ij}\| + \|r_{ij}\|) < 0 \quad (19)$$

E. System Architecture

In this subsection, will be described how to implement the new algorithm into a robot. The VS approach needs a special architecture that can perform those three steps. So, the system architecture is built by using three hierarchical layers: a consensus tracking module, a consensus-based formation control module, and the physical robot control module. The elaboration of virtual structure approach into architecture for formation control with obstacle/collision avoidance system is shown in Figure 8.

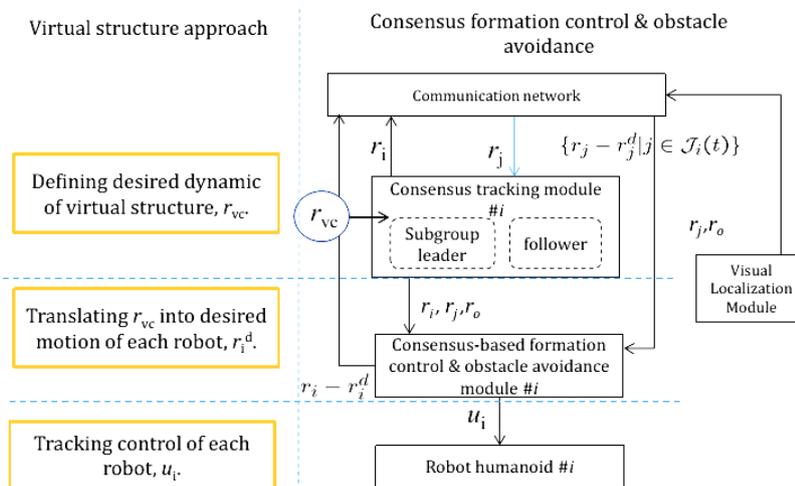


Figure 8. The elaboration of VS approach into distributed architecture for obstacle/collision avoidance and formation control [3]



Figure 9. Aldebaran's Nao robots for the experiment

Figure 9 shows the robot which was used in the experiment. The robots used for experiment are Nao robot from Aldebaran Robotic, France.

IV. RESULT AND DISCUSSION

In this section, some simulation and experiment results of the application of the proposed equation on a group of humanoid robots were presented. As mentioned before, robot's dynamics is assumed as a single integrator system.

For simulation and experiment, 3 robots are placed in the left side of the experiment area and 1 robot on the right. An obstacle also placed randomly in the middle of the area. The group of robots walk to their destination on the right side and the 4th robot walks to left side of the experiment area.

A. Simulation Result

Simulations were performed on 4 agents, representing 4 robots, using topology in Figure 3. The initial position of Robot1, Robot2, Robot3, and Robot4 are, respectively, $r_{R1} = [0.7300, 1.1905]$, $r_{R2} = [-0.0081, 1.2198]$, $r_{R3} = [-0.0149, 0.4276]$, and $r_{R4} =$

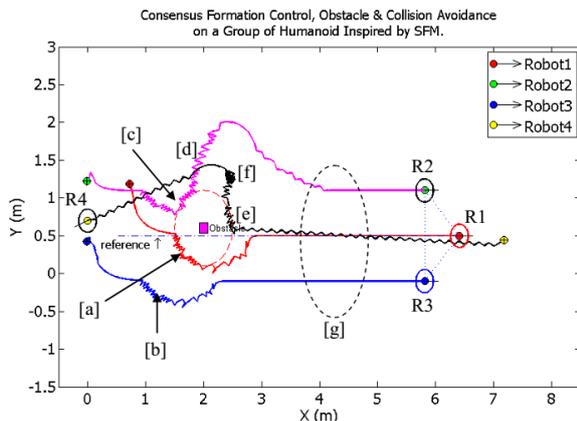


Figure 10. Simulation result

$[7.1790, 0.4428]$; while the obstacle is placed at position $r_{Obst} = [2, 0.6]$. All these positions are obtained by using VO, which the algorithm is depicted in Figure 6. As seen in Figure 9, all robots wear a marker on their head. Figure 10 shows the simulation result of the proposed algorithm.

The result shows that when Robot1 met the safety barrier (R_{safe}), it started to avoid the obstacle. During Robot1 was avoiding the obstacle (point [a]), Robot2, and Robot3, also perform an avoidance maneuvers, although there is no obstacle in front of them. This is because the consensus term has worked while the avoidance term has not active yet. This can be seen in the behavior of Robot3, as shown in point [b].

At point [c], it is shown that Robot2 is following the formation of Robot1, but must meet the R_{safe} of the obstacle. Robot2 reacts to turn left, but at point [d] he met with dynamic obstacle (Robot4). The reaction of Robot3 is keeping its maneuver by continuing to turn left, while Robot4 being avoiding static obstacle turn to the right [e].

As result, the two robots constantly avoiding each other, until at some point one of them sense the absence of the obstacle. It's shown in point [f], where Robot4 and Robot3 sensed the absence of the obstacle. Robot4 was continuing its mission towards point $[0, 0.6]$ and Robot3 was returning back to its formation [g].

B. Experiment Result

Experiments were performed on 4 Nao robot, using topology in Figure 3. An ASUS RT-N10 router, a Genius F-120 web camera and a computer were used to perform the experiment. The video of this experiment can be watched on Youtube channel [11]. The experiment result is depicted in Figure 11 showing that the experiment result also get a similar result to the simulation.

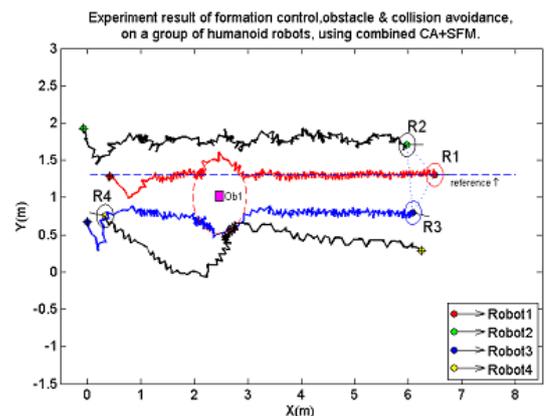


Figure 11. Experiment result

V. CONCLUSION

In this research, a new algorithm for obstacle and collision avoidance on a group of humanoid robots inspired by SFM is successfully developed. Stability analysis on the new algorithm has proved that algorithm can make a group of humanoid robots avoid obstacle. Comparing to our previous results, this algorithm has a smoother avoidance maneuver and faster to return to its formation. It also found in this study that the CA part on the algorithm is succeeded to maintain the position of the robot back to its formation. In the case of robot is trapped in a crowded situation (singularity condition), robot will still trying to look a new position, until it find a condition that allow him to move forward.

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